



# Multi-Functional Flexible Planar Hall Effect Sensors

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Shai Amrusi<sup>2</sup>, Asaf Grosz<sup>2</sup> and Lior Klein<sup>1</sup>

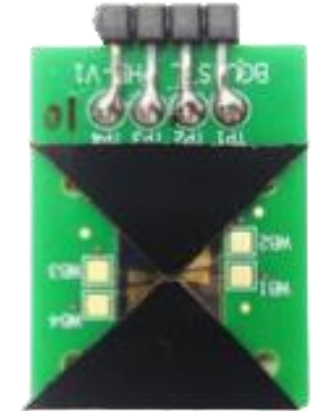
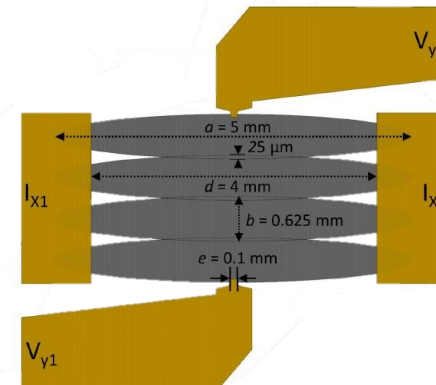
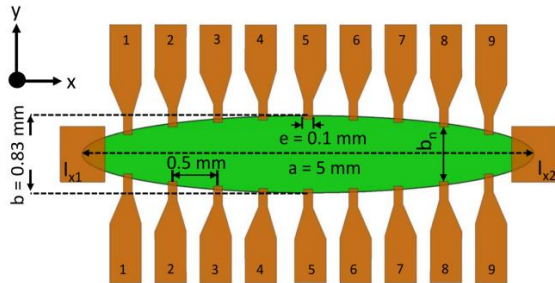
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# Planar Hall Effect Sensors

## Configurations and Best Magnetic Resolutions:

- PHE Sensor without Magnetic Flux Concentrators: 24 pT/ $\sqrt{\text{Hz}}$  at 50 Hz.
- PHE Sensor with Magnetic Flux Concentrators: 5 pT/ $\sqrt{\text{Hz}}$  at 10 Hz.
- PHE Sensor Array (4 Ellipses): 16 pT/ $\sqrt{\text{Hz}}$  at 100 Hz.
- Gradiometer Configuration: 26 pT/mm/ $\sqrt{\text{Hz}}$  at 50 Hz.
- **Flexible PHE Sensor:** Better than 200 pT/ $\sqrt{\text{Hz}}$  at 10 Hz.



# Planar Hall Effect Sensors

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## Potential Areas of Applications:

- **Automotive Industry:** Ideal for applications requiring a dynamic range exceeding 100 Oe, with expected resolutions in the nano-tesla range, making it suitable for advanced vehicle technologies.
- **Lab-on-Chip Systems:** Published studies highlight the superior performance of PHE sensors compared to previously utilized xMR sensors, offering enhanced capabilities for compact, integrated lab systems.
- **Flexible Electronics:** Highly applicable in fields such as soft robotics, consumer electronics, healthcare devices, and more.
- **Strain Gauges:** Have the potential to function as ultra-sensitive strain gauges capable of detecting micro-strain variations down to a few percent.



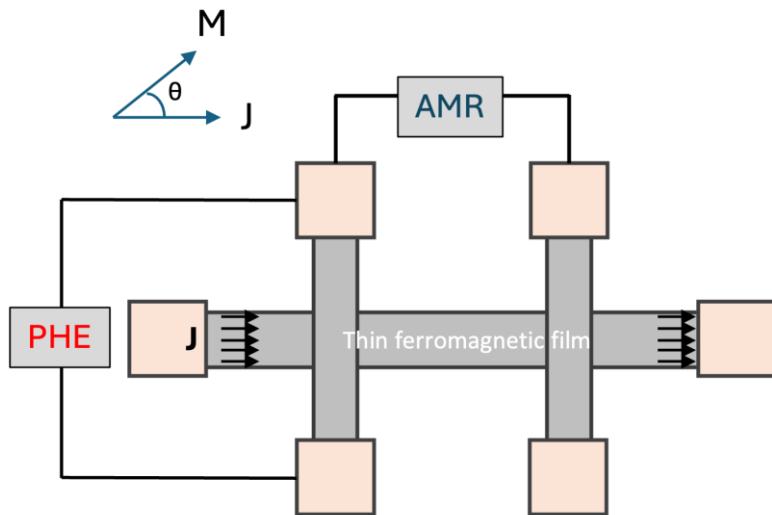
Article

## Planar Hall Effect Magnetic Sensors with Extended Field Range

Daniel Lahav <sup>1</sup>, Moty Schultz <sup>1</sup>, Shai Amrusi <sup>2</sup>, Asaf Grosz <sup>2</sup> and Lior Klein <sup>1,\*</sup>

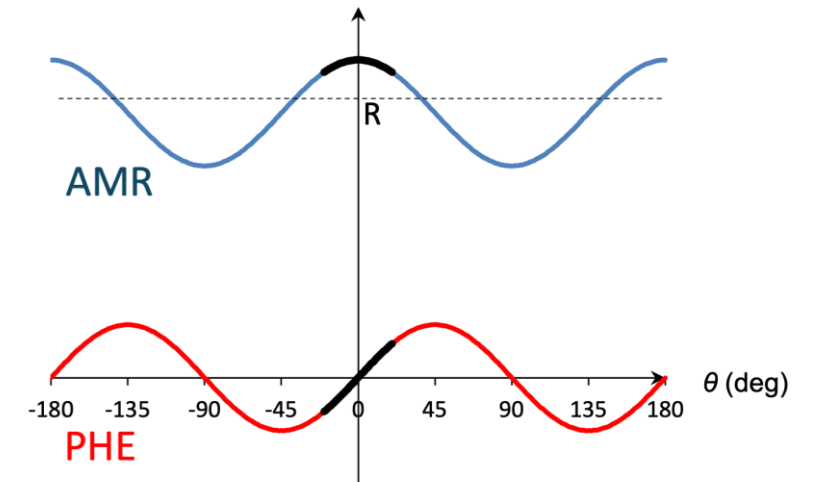


# AMR and PHE



$$\rho_{xx} = \rho_{\perp} + (\rho_{\parallel} - \rho_{\perp}) \cos^2 \theta$$

$$\rho_{xy} = 0.5 \cdot (\rho_{\parallel} - \rho_{\perp}) \sin 2\theta$$

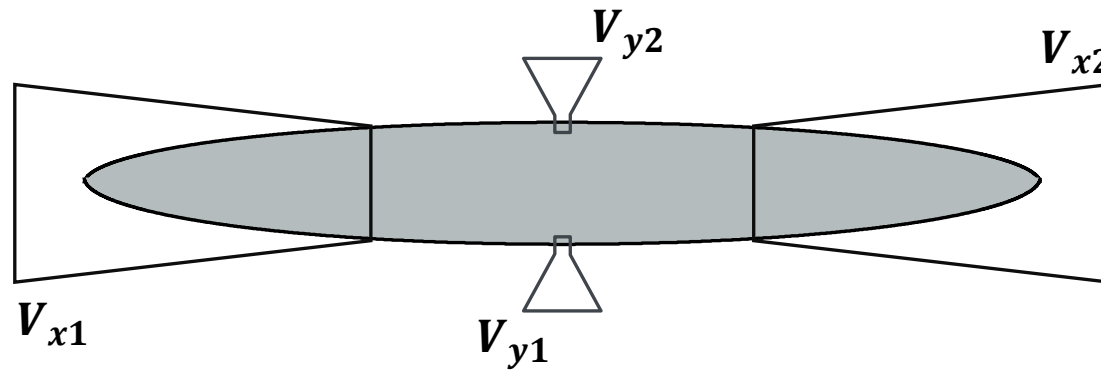


# Elliptical PHE Sensors

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## Why Elliptical?

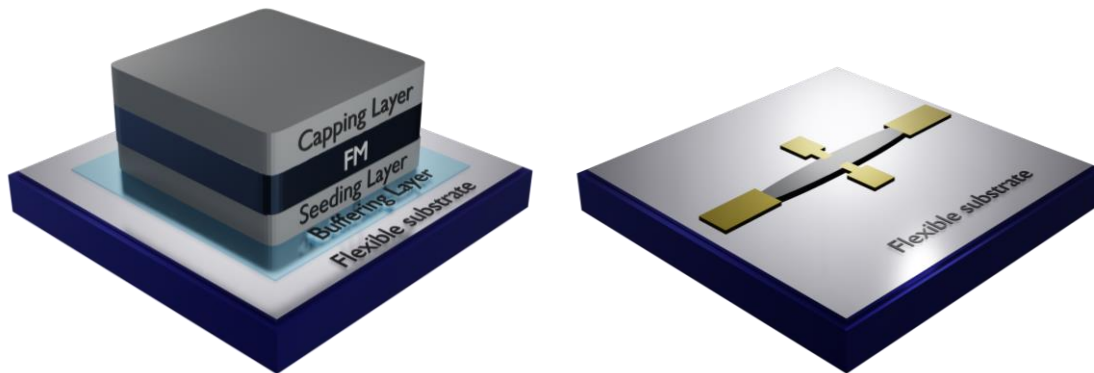
- Stable uniform magnetization (shape anisotropy).
- Low anisotropy fields (higher signal).



# Flexible EPHE Sensors

## Materials and Layer Stack

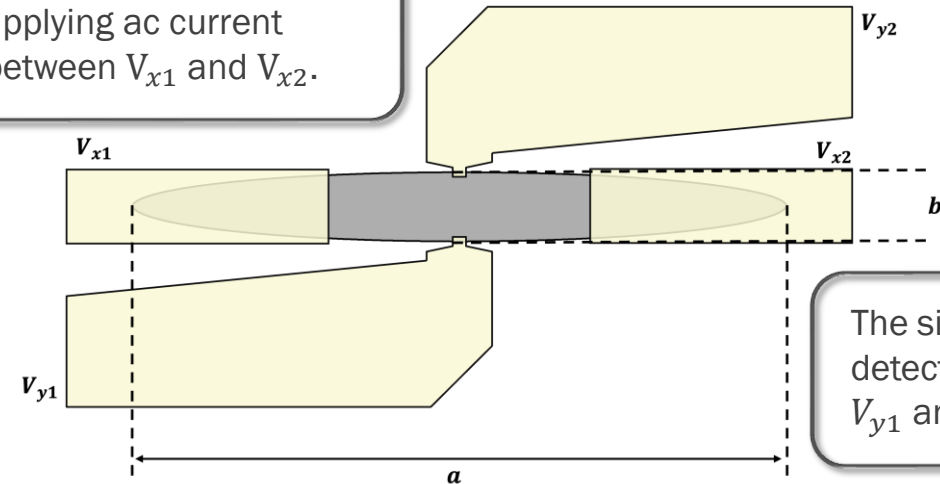
- **Permalloy ( $\text{Py}, \text{Ni}_{80}\text{Fe}_{20}$ )** – FM layer, due to its low MCA coefficient, high permeability, and low coercive field.
- **Tantalum (Ta)** - Dual purpose as a seeding layer and a capping layer.
- **Aluminum oxide ( $\text{Al}_2\text{O}_3$ )** – Buffering layer.
- **Kapton tape**– Serves as a flexible substrate.
- **SU-8 TF 6002** – For surface smoothening.



## Device Design

- Elliptical PHE sensor - aspect ratio 1:8.
  - Major axis ( $a$ ) – 5 mm.
  - Minor axis ( $b$ ) – 625  $\mu\text{m}$ .
- Flexible substrate thickness – 125  $\mu\text{m}$ .

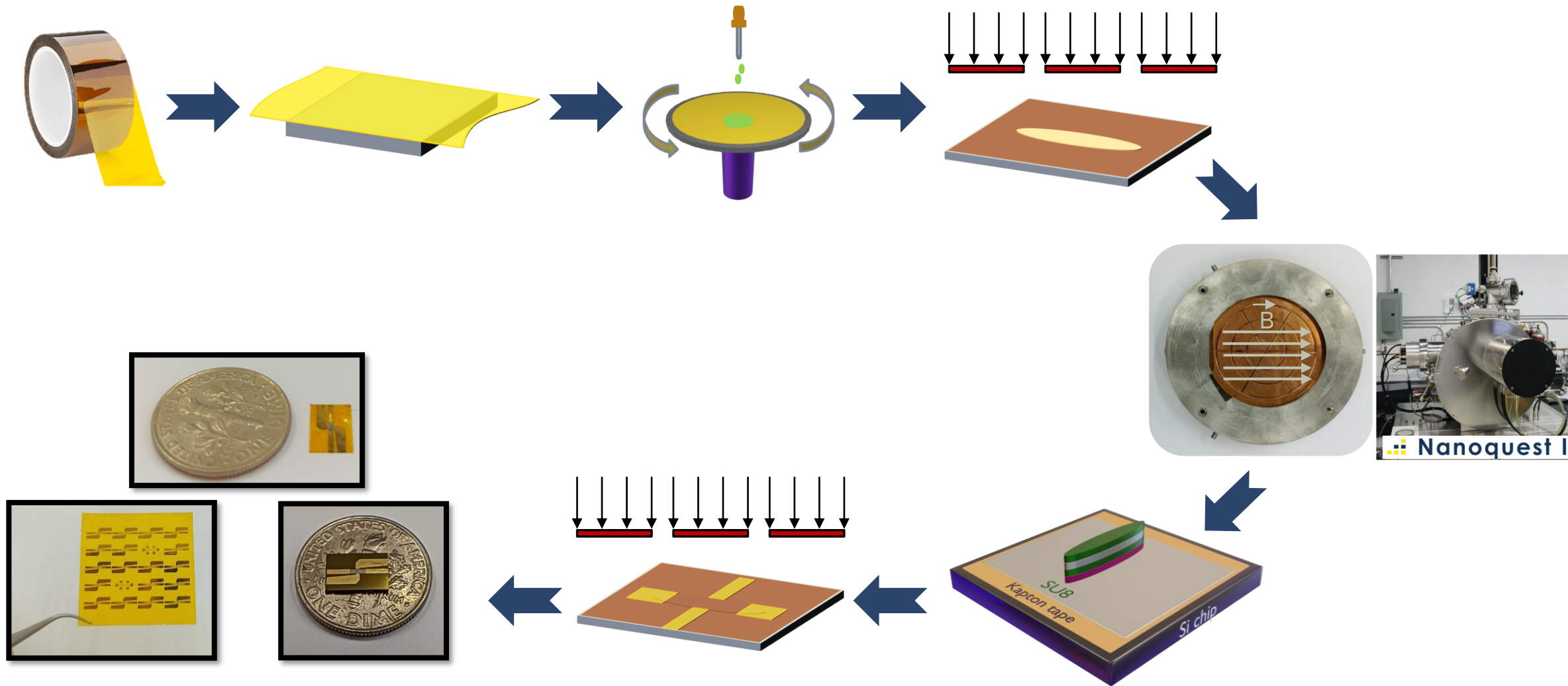
The sensor is excited by applying ac current between  $V_{x1}$  and  $V_{x2}$ .



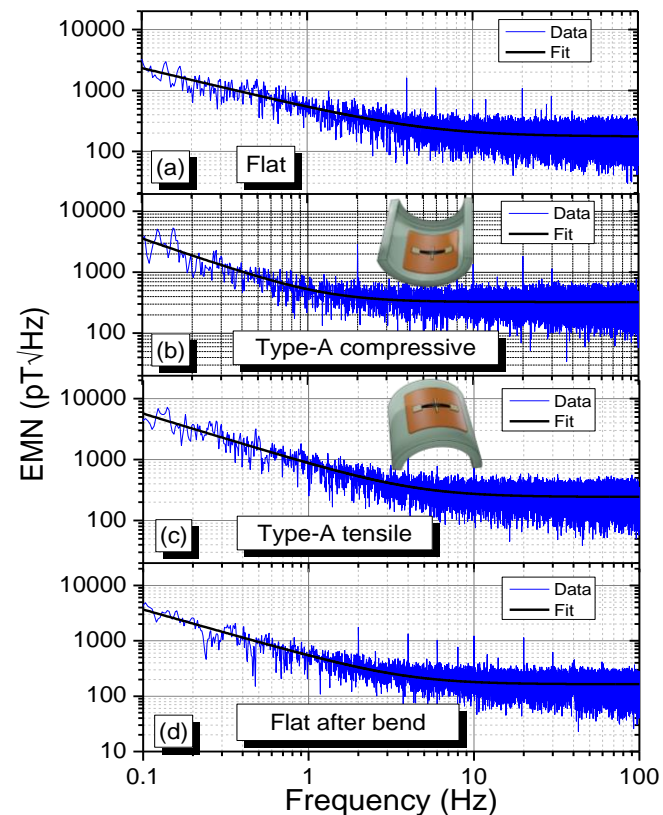
The signal is detected between  $V_{y1}$  and  $V_{y2}$ .



# Fabrication Process

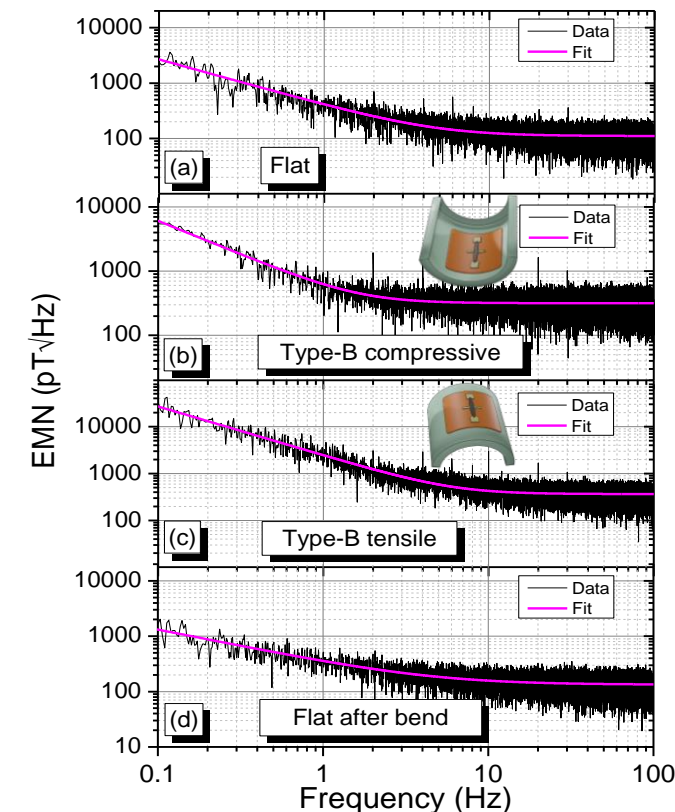


# Sub-200 pT Resolution of Flexible EPHE Sensors



Mode	100 Hz ( $\text{pT}/\sqrt{\text{Hz}}$ )	10 Hz ( $\text{pT}/\sqrt{\text{Hz}}$ )	1 Hz ( $\text{pT}/\sqrt{\text{Hz}}$ )	0.1 Hz ( $\text{pT}/\sqrt{\text{Hz}}$ )
Flat	177	209	544	2335
Type-A compressive	244	273	876	5684
Type-A tensile	323	327	524	3557
Flat after-bent	164	179	547	3669
Flat	111	125	414	2664
Type-B compressive	317	320	628	6050
Type-B tensile	365	426	2467	26975
Flat after-bent	134	157	358	1317

Among the best reported values for flexible magnetic sensors.





# Flexible EPHE Sensors Under Bending Conditions

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## Strain Anisotropy

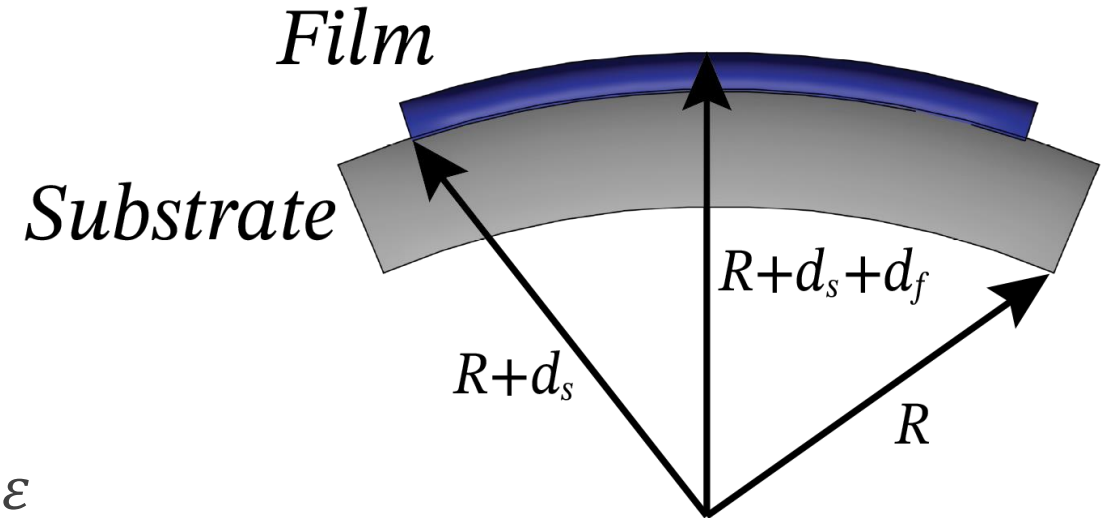
$$\varepsilon = \frac{d_f + d_s}{2R}$$

Strain anisotropy constant:

$$K_\sigma = \frac{3}{2} \frac{Y_f \lambda_s}{1 - \nu^2} \varepsilon$$

Strain anisotropy field:

$$H_\sigma = \frac{2K_\sigma}{M_s} = \frac{3Y_f \lambda_s}{(1 - \nu^2)M_s} \varepsilon$$



# Flexible EPHE Sensors Under Bending Conditions

## The Effect of Bending on the Effective Anisotropy Field

Mode	$H_{\text{eff}}$ (Oe)
Flat	7.2
Type-A compressive	7.8
Type-A tensile	17.8
Flat after-bent	6.6
Flat	6.7
Type-B compressive	14.0
Type-B tensile	7.8
Flat after-bent	7.5

$H_{\text{eff}}^{(f)}$  points to the 'Flat' row (7.2 Oe).  
 $H_{\text{eff}}^{(i)}$  points to the 'Type-A compressive' row (7.8 Oe).

$$\begin{aligned} H_{\text{eff}}^{(i)} &= H_{\text{int}} \\ H_{\text{eff}}^{(f)} &= H_{\text{int}} + H_{\sigma} \end{aligned} \Rightarrow \delta H = H_{\text{eff}}^{(f)} - H_{\text{eff}}^{(i)} = H_{\sigma}$$

Flexible EPHE sensors can measure both magnetic fields and strains simultaneously **under the application of an external field.**

# Multi-Functional Flexible EPHE Sensor

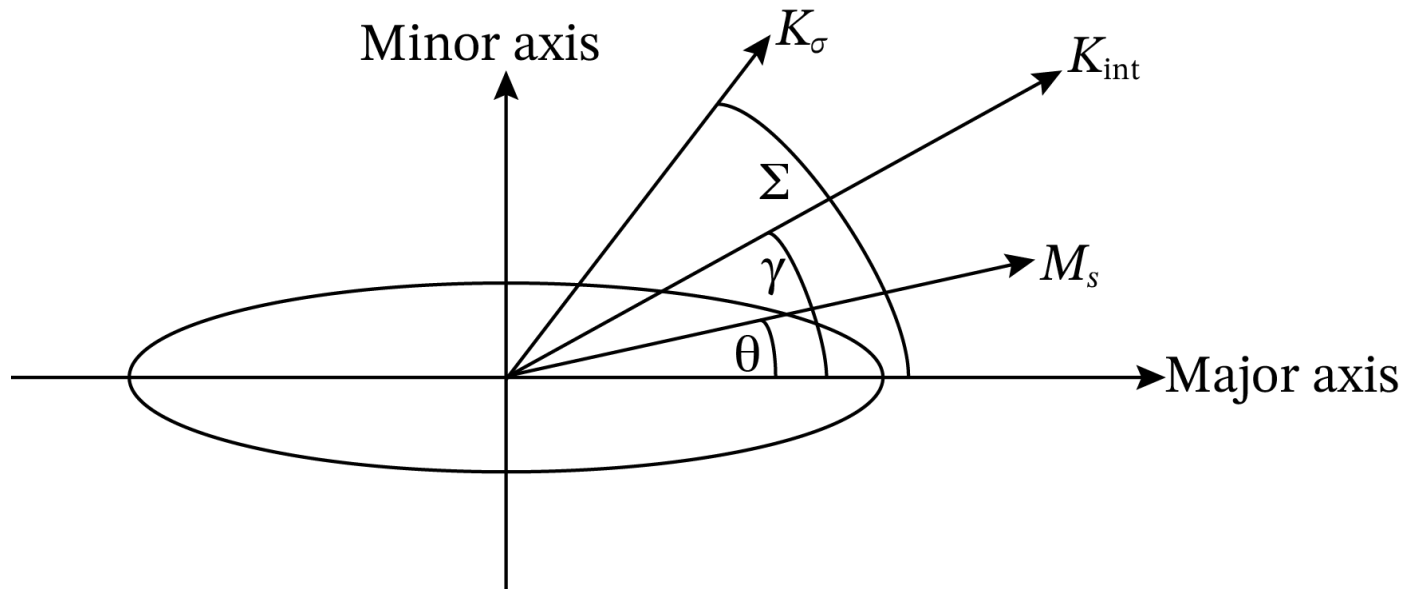
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- ☐ Can minute strain be measured with a flexible EPHE sensor without the reliance on an external magnetic field?

# Introducing a Tunable Anisotropy Landscape

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$$E = K_{\text{int}} \sin^2(\gamma - \theta) + K_{\sigma} \sin^2(\Sigma - \theta)$$



# Multi-Functional Flexible EPHE Sensor

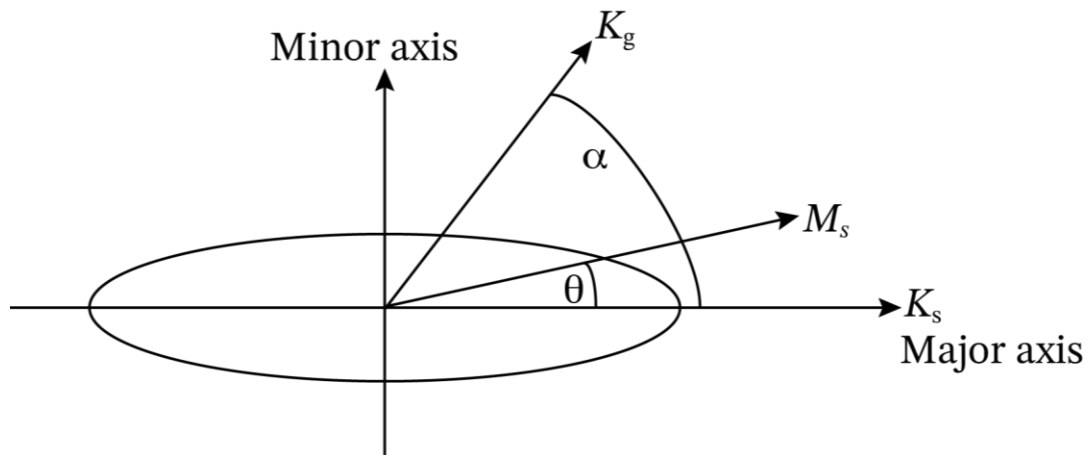
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- ☒ Can minute strain be measured with a flexible EPHE sensor without the reliance on an external magnetic field?
- ☐ Is it feasible to fabricate a device that meets these requirements?

# Tuning the Easy Magnetization Direction

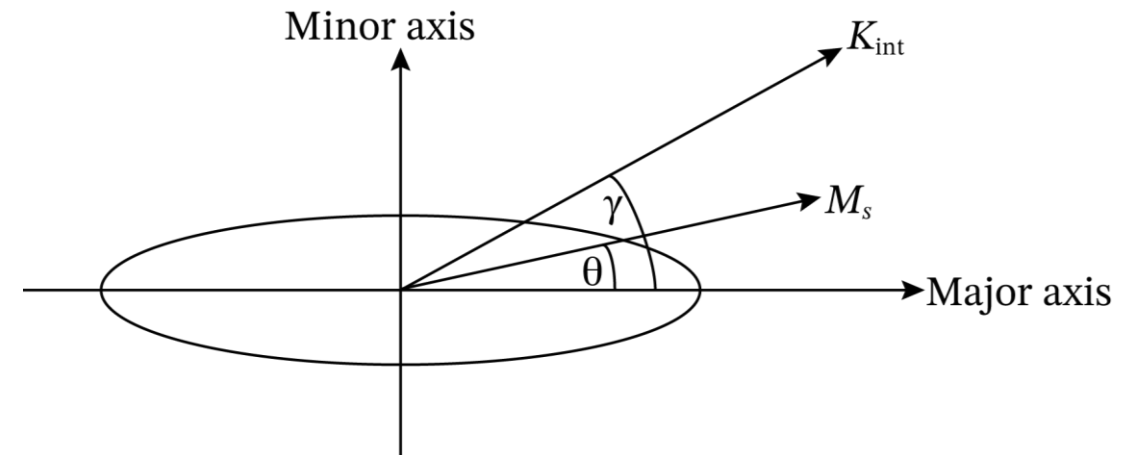
## Balancing Shape and Growth Anisotropies

$$E = K_g \sin^2(\alpha - \theta) + K_s \sin^2(\beta - \theta)$$



## The Resulting Equilibrium

$$E = K_{\text{int}} \sin^2(\gamma - \theta)$$





# Multi-Functional Flexible EPHE Sensor

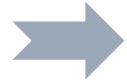
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- ☒ Can minute strain be measured with a flexible EPHE sensor without the reliance on an external magnetic field?
- ☒ Is it feasible to fabricate a device that meets these requirements?
- ☐ What is the expected strain-gauge resolution for such a device?

# Expected Strain Gauge Resolution

$$\Delta\theta = \kappa \cdot \Delta\varepsilon$$

$$\Delta V = \lambda \cdot \Delta\theta$$



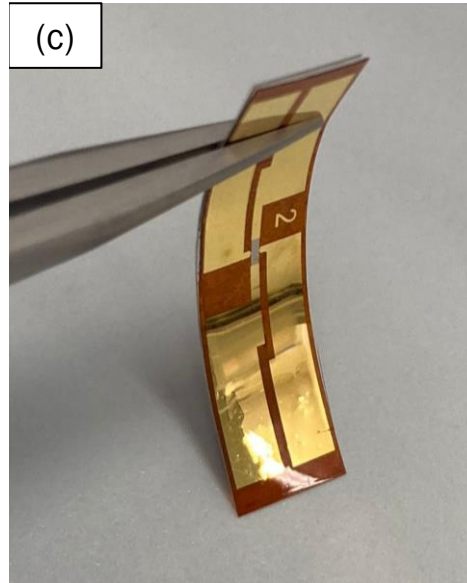
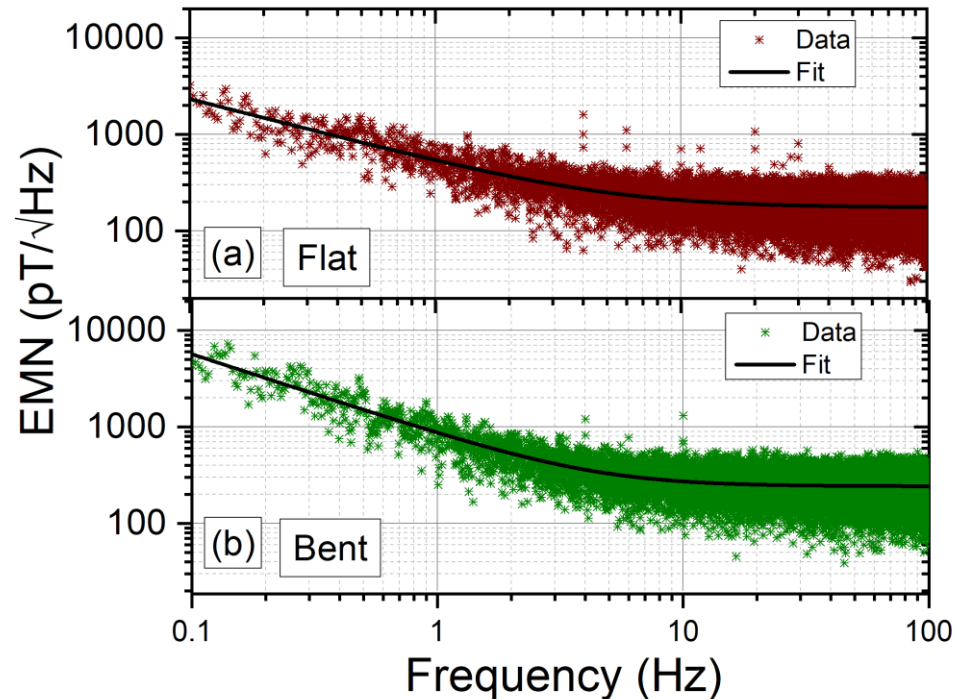
$$\Delta\varepsilon = \frac{\Delta V}{\lambda \cdot \kappa}$$



$$\varepsilon_{\min} = \frac{\Delta V_{\min}}{\lambda \cdot \kappa}$$



$$B_{\min} = \frac{\Delta V_{\min}}{S_y}$$



Minimum detectable strain

$$\varepsilon_{\min} \approx 2 \cdot 10^{-8}$$

# Multi-Functional Flexible EPHE Sensor

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- ☑ Can minute strain be measured with a flexible EPHE sensor without the reliance on an external magnetic field?
- ☑ Is it feasible to fabricate a device that meets these requirements?
- ☑ What is the expected strain-gauge resolution for such a device?

# Conclusions

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- **Multi-Functional Capability:** Our flexible EPHE sensors go beyond magnetic field detection, demonstrating their ability to act as strain gauges capable of detecting micro-strain with exceptional sensitivity.

Thank you!

# Sensitivity and Noise

## Sensitivity

$$S_y = \frac{V_y}{H_y} = I_x \frac{\Delta\rho}{t} \frac{1}{H_{\text{eff}}}$$

Bias current  $\rightarrow I_x$

Resistivity anisotropy  $(\Delta\rho = \rho_{\parallel} - \rho_{\perp}) \rightarrow \Delta\rho$

Sensor thickness  $\rightarrow t$

Effective anisotropy  $\rightarrow H_{\text{eff}}$

## Equivalent magnetic noise (EMN)

$$\text{EMN}(f) = \frac{e_{\Sigma}(f)}{S_y} = \frac{\sqrt{e_{1/f}^2 + e_T^2 + e_{\text{amp}}^2}}{I_x \frac{\Delta\rho}{t} \frac{1}{H_{\text{eff}}}}$$

$\sqrt{e_{1/f}^2 + e_T^2 + e_{\text{amp}}^2}$  is the sum of noise components:

- $e_{1/f}$ : 1/f noise
- $e_T$ : Thermal noise
- $e_{\text{amp}}$ : Amplifier noise

The denominator is the same as in the sensitivity equation:  $I_x \frac{\Delta\rho}{t} \frac{1}{H_{\text{eff}}}$

# Flexible EPHE Sensors Under Bending Conditions

## Strain Anisotropy

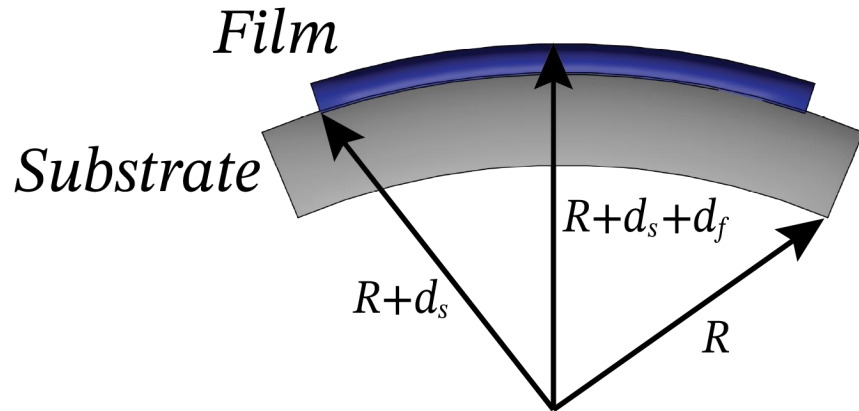
$$\varepsilon = \frac{d_f + d_s}{2R}$$

Strain anisotropy constant:

$$K_\sigma = \frac{3}{2} \frac{Y_f \lambda_s}{1 - \nu^2} \varepsilon$$

Strain anisotropy field:

$$H_\sigma = \frac{2K_\sigma}{M_s} = \frac{3Y_f \lambda_s}{(1 - \nu^2)M_s} \varepsilon$$



## Anisotropy Landscape

The effective anisotropy ( $H_{\text{eff}}$ ) represents the combined influence of the sensor's intrinsic properties and external effects.

- The intrinsic anisotropy ( $H_{\text{int}}$ ) define the sensor's fundamental and stable anisotropic properties, which remain fixed after fabrication.
  - Shape anisotropy ( $H_s$ ).
  - Growth-induced anisotropy ( $H_g$ ).
- External effects - dynamically modify the anisotropy landscape during the sensor's operation.
  - Strain-Induced Anisotropy ( $H_\sigma$ ).

$$E = K_s \sin^2 \vartheta + K_g \sin^2 \phi + K_\sigma \sin^2 \Sigma$$

$\Downarrow$

$$E = K_{\text{int}} \sin^2 \gamma + K_\sigma \sin^2 \Sigma$$

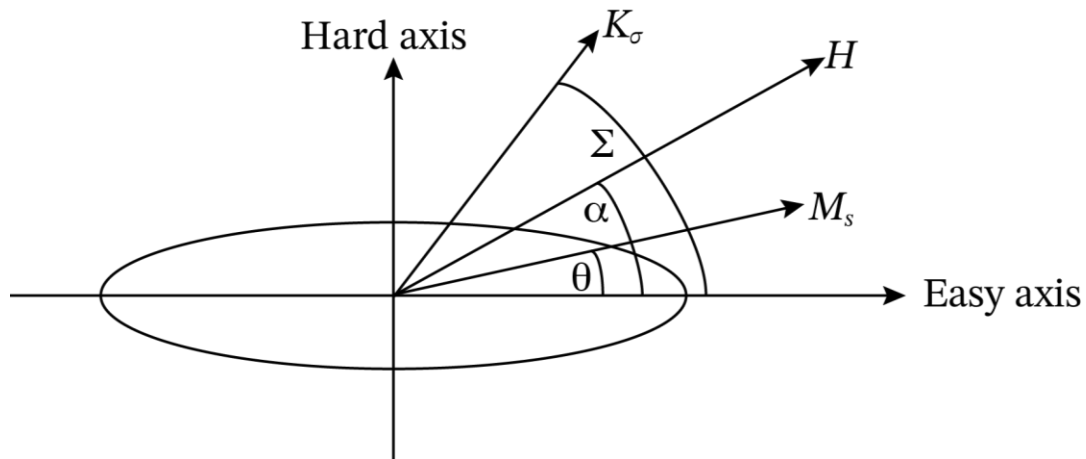


# Flexible EPHE Sensors Under Bending Conditions

## Modified Stoner-Wohlfarth model

- SW Model - A theoretical model describing the behavior of single domain particles under an external magnetic field.
- Modified SW Model - Incorporates both intrinsic MA and strain-induced anisotropy.

$$E = K_{\text{int}} \sin^2 \theta + K_{\sigma} \sin^2(\Sigma - \theta) - M_s H \cos(\alpha - \theta)$$



## The effect of bending on the effective anisotropy field

Mode	$H_{\text{eff}}$ (Oe)
Flat	7.2
Type-A compressive	7.8
Type-A tensile	17.8
Flat after-bent	6.6
Flat	6.7
Type-B compressive	14.0
Type-B tensile	7.8
Flat after-bent	7.5

$$H_{\text{eff}}^{(i)} = H_{\text{int}} \Rightarrow \delta H = H_{\text{eff}}^{(f)} - H_{\text{eff}}^{(i)} = H_{\sigma} = \frac{3Y_f \lambda_s}{(1 - \nu^2)M_s} \varepsilon$$

$$H_{\text{eff}}^{(f)} = H_{\text{int}} + H_{\sigma}$$

Flexible EPHE sensors can measure both magnetic fields and strains simultaneously **under the application of an external field.**

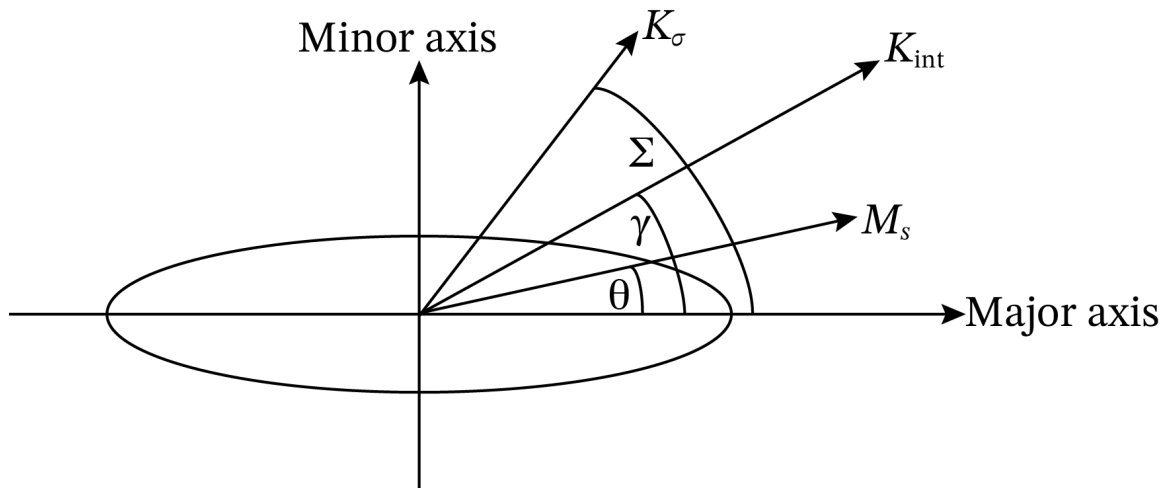
# Introducing a Tunable Anisotropy Landscape

## Energy Landscape and PHE signal:

- The total energy of the system is given by:

$$E = K_{\text{int}} \sin^2(\gamma - \theta) + K_{\sigma} \sin^2(\Sigma - \theta)$$

- Strain is applied solely along the principal axes ( $\Sigma_1 = 0^\circ$  and  $\Sigma_2 = 90^\circ$ ) to **maximize its impact on the anisotropy** landscape and ensure a **predictable, simplified** response.



## Optimal angle for maximizing the PHE signal

- The PHE signal is proportional to  $\sin 2\theta$ , and the change in the signal due to strain is:

$$\Delta V_{\text{PHE}} \propto |\sin 2\theta_{\text{min},1} - \sin 2\theta_{\text{min},2}|$$

- To maximize  $\Delta V_{\text{PHE}}$ ,  $\gamma$  must be chosen such that the perturbation results in the largest relative shift between  $\theta_{\text{min},1}$  and  $\theta_{\text{min},2}$ .

Through analysis,  $\gamma = 22.5^\circ$  is found to be the optimal angle for the intrinsic anisotropy.